



# Design, Modeling, and Control of a Flying-Insect-Inspired Quadrotor with Rotatable Arms

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## Background

Quadrotors have become very popular in aerial manipulation and delivery, but they have experienced a common technical issue: the center of gravity (CoG) is usually offset from the symmetric center of the quadrotor due to the eccentric payloads carried. When the CoG of a conventional quadrotor with fixed arms (QFA) is offset from its symmetric center, the QFA suffers from two issues:

- Decreased stability
- Increased power consumption



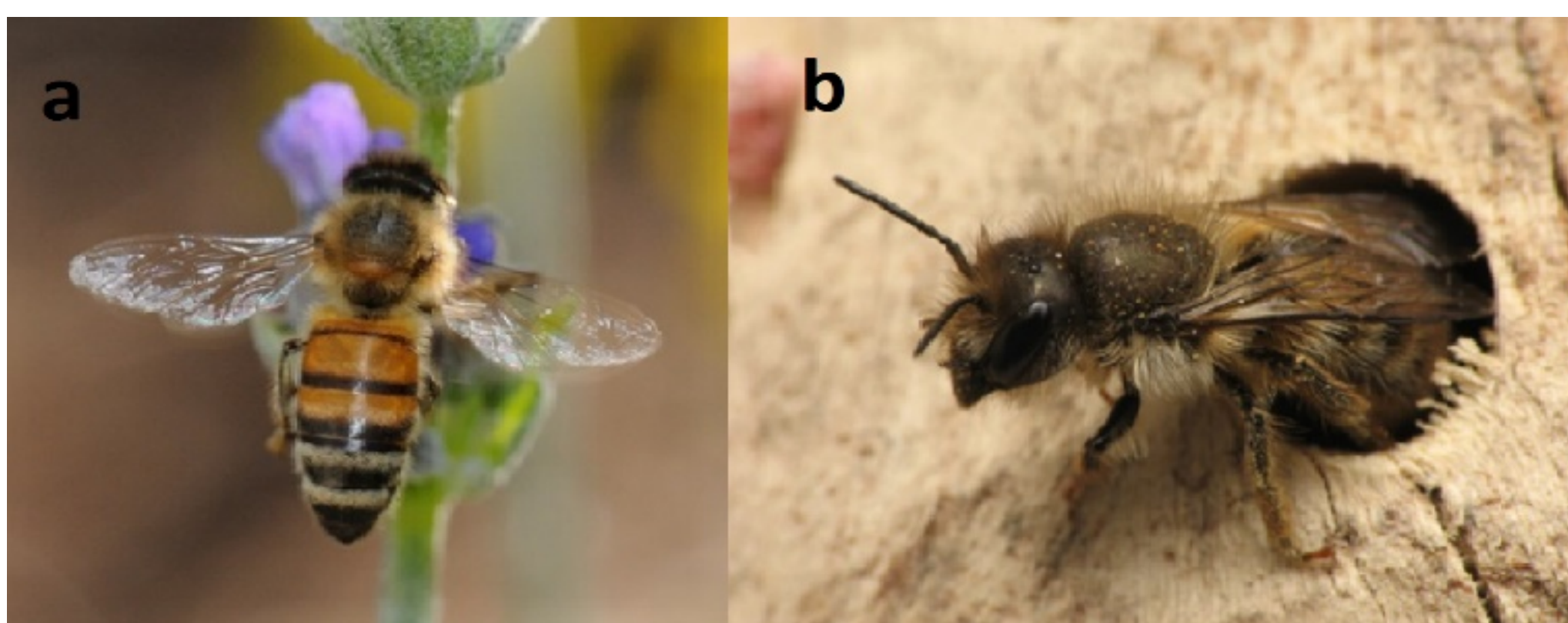
Aerial manipulation



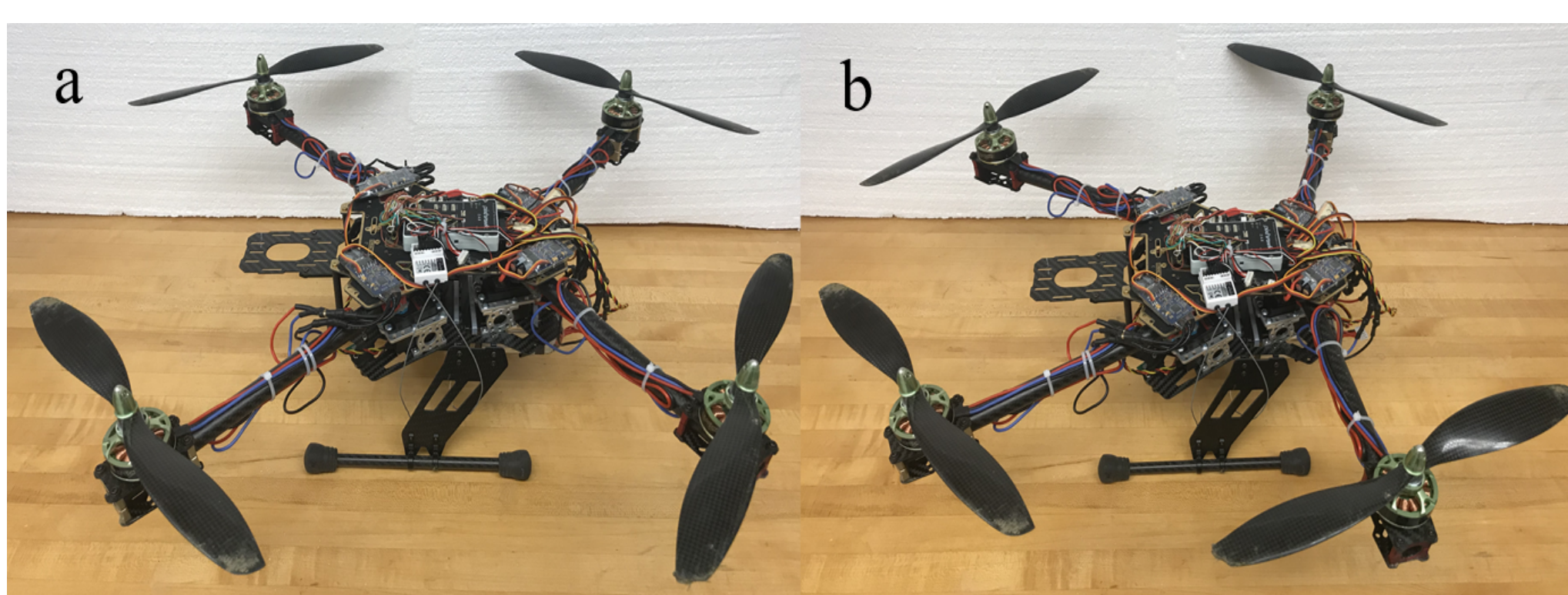
Aerial delivery

## Objectives

Inspired by flying insects (e.g., bees) that expand their wings when flying and hide them when crawling, a quadrotor with rotatable arms (QRA) is proposed. By rotating arms, a QRA can move its symmetric center to its CoG while still keeping all rotor thrusts the same during flight. In this way, the stability and energy efficiency of the QRA can be improved in hovering or low-speed translation, compared to a QFA with the same arms, weight, rotors, and eccentric payloads.

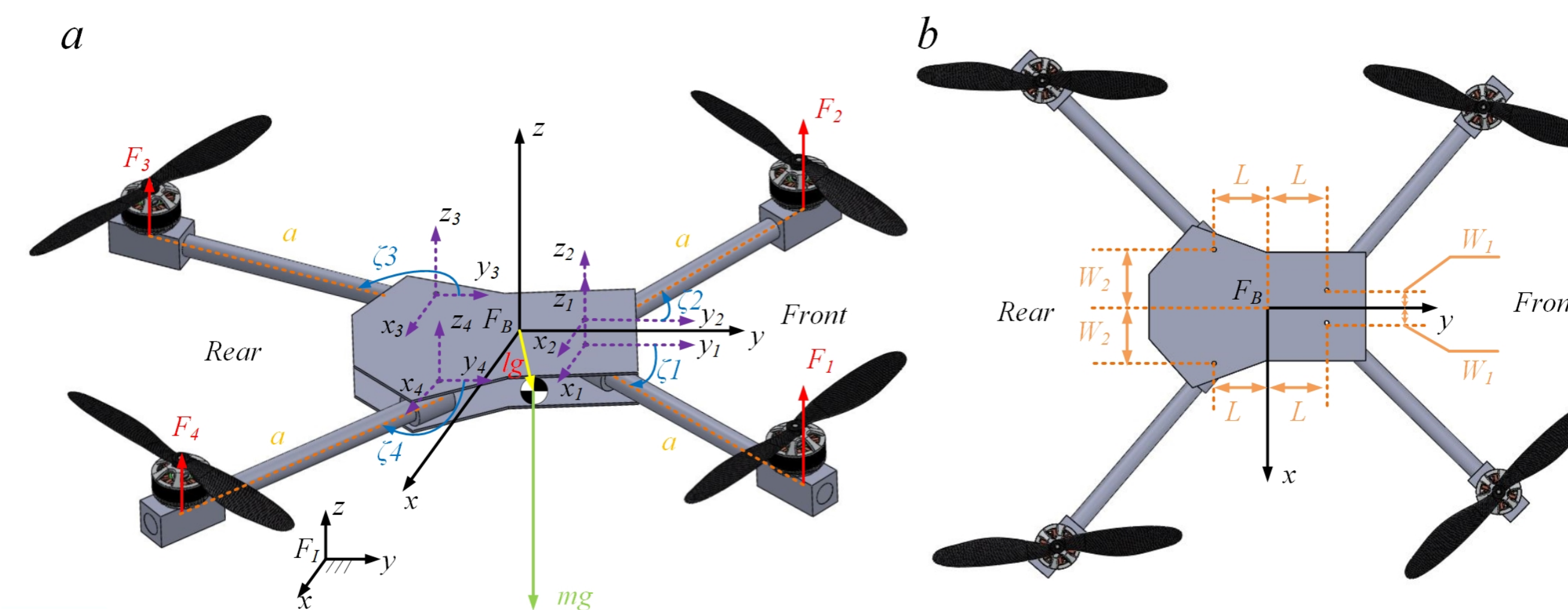
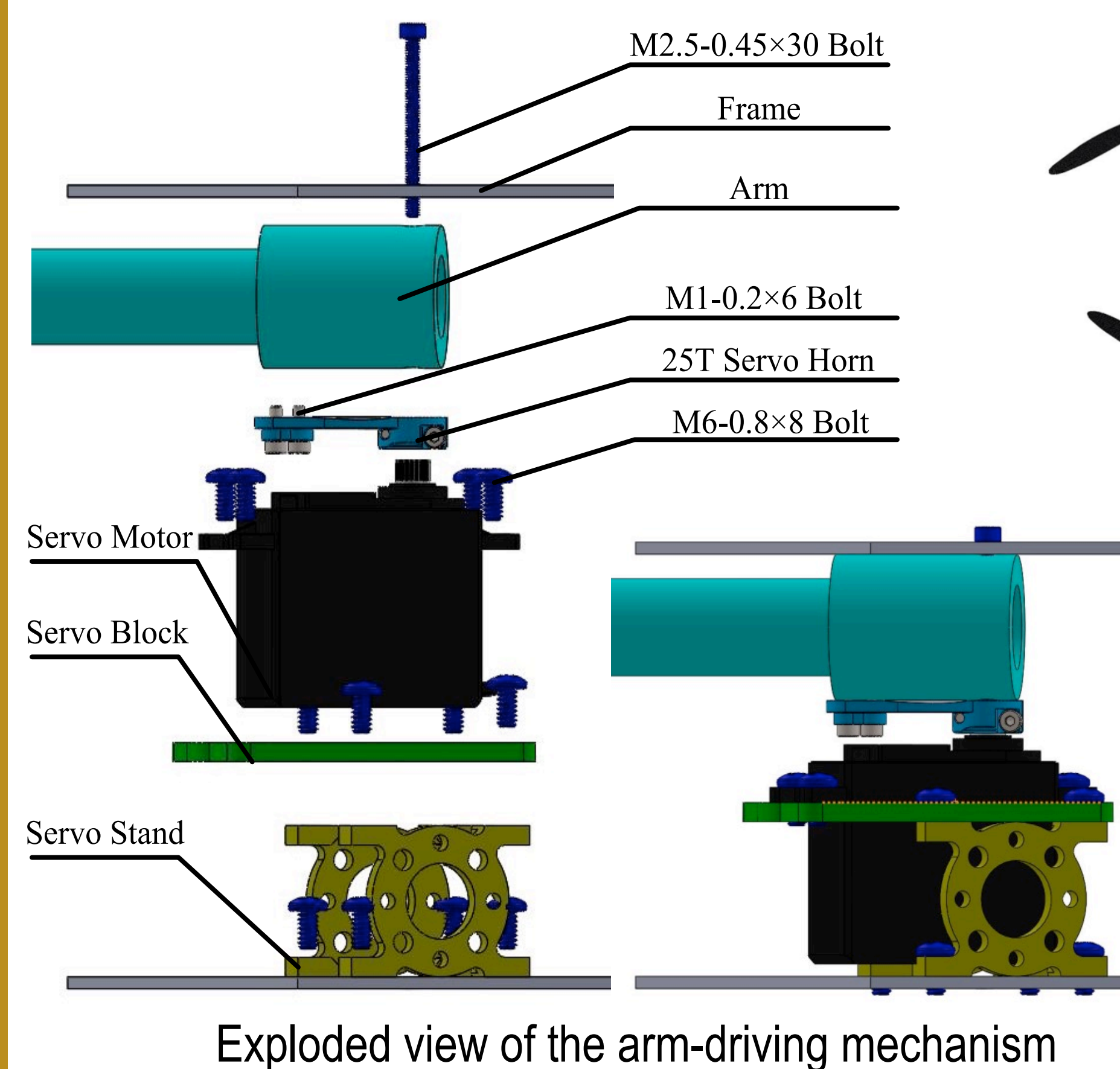


A bee with (a) expanded wings and (b) folded wings



(a) A QRA prototype; and (b) Arms of the QRA are rotatable

## Prototype Design and Dynamics Modeling

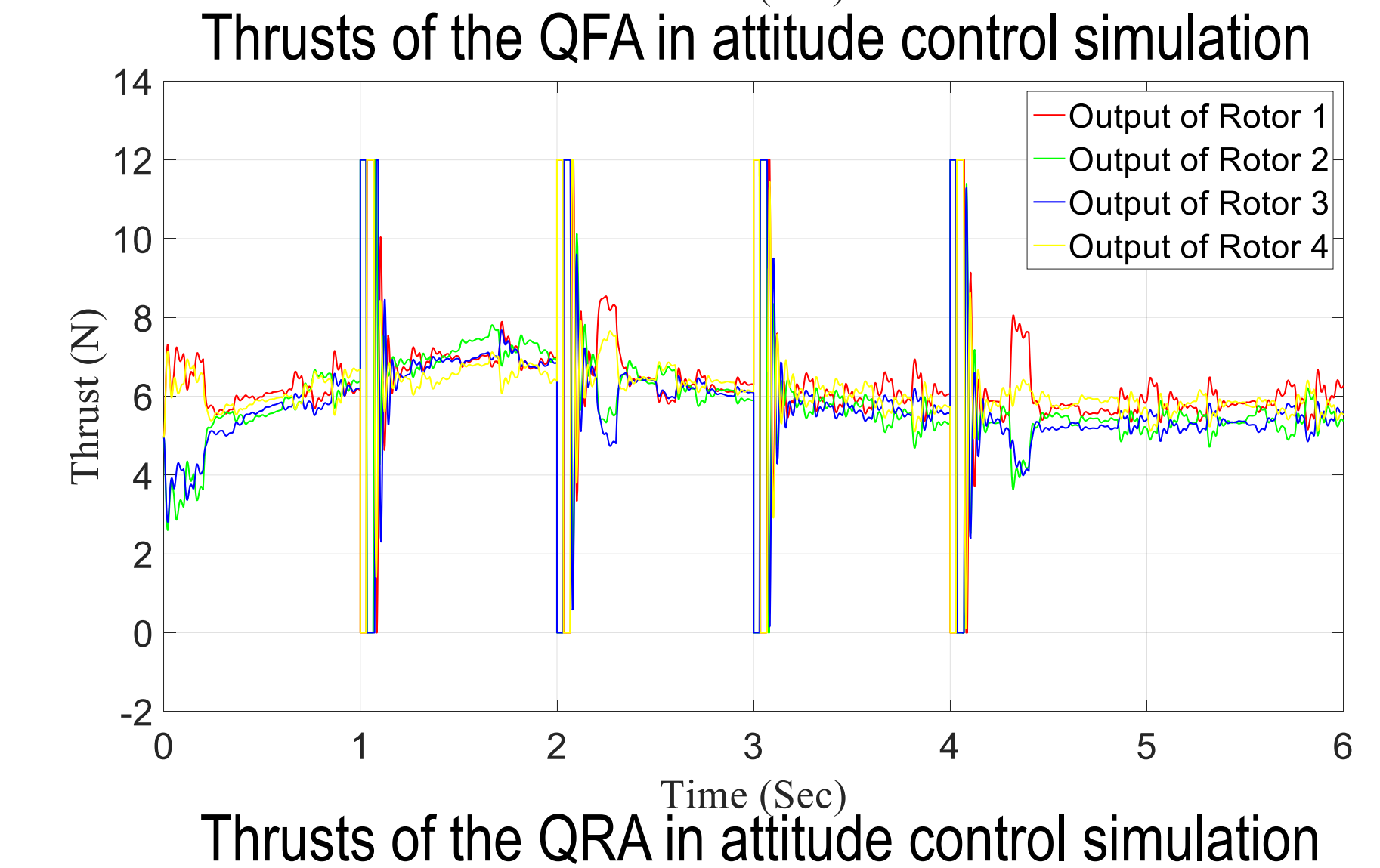
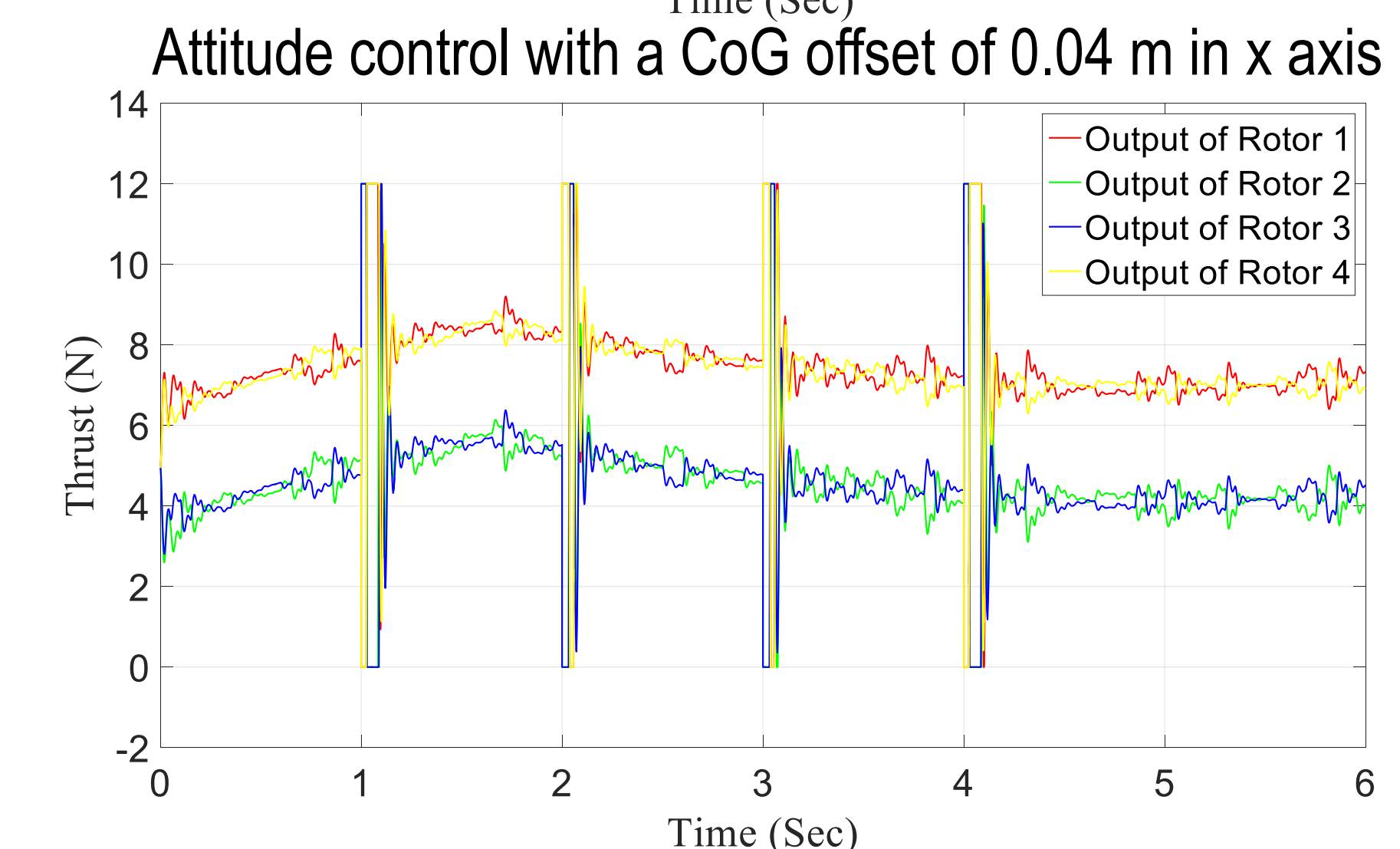
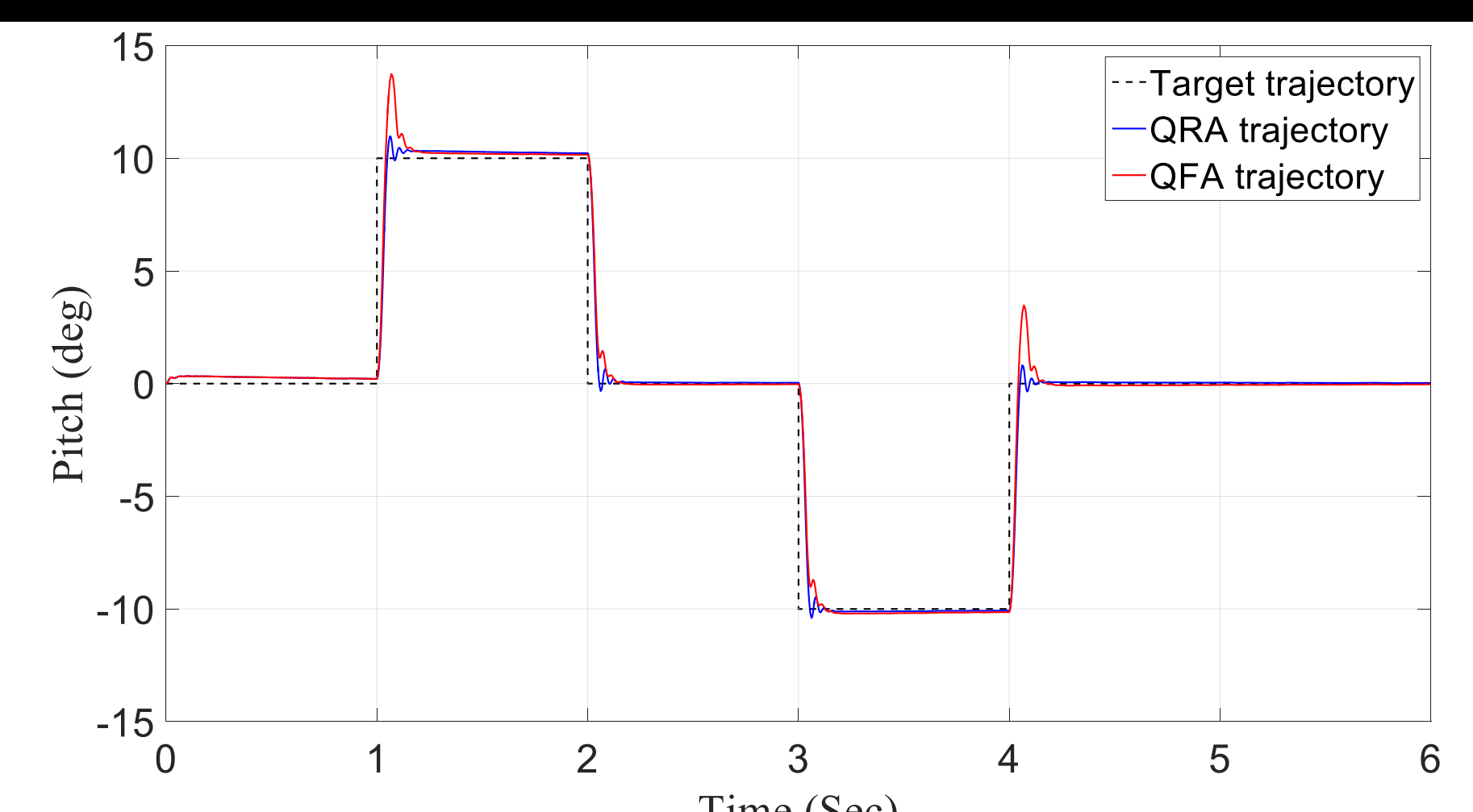
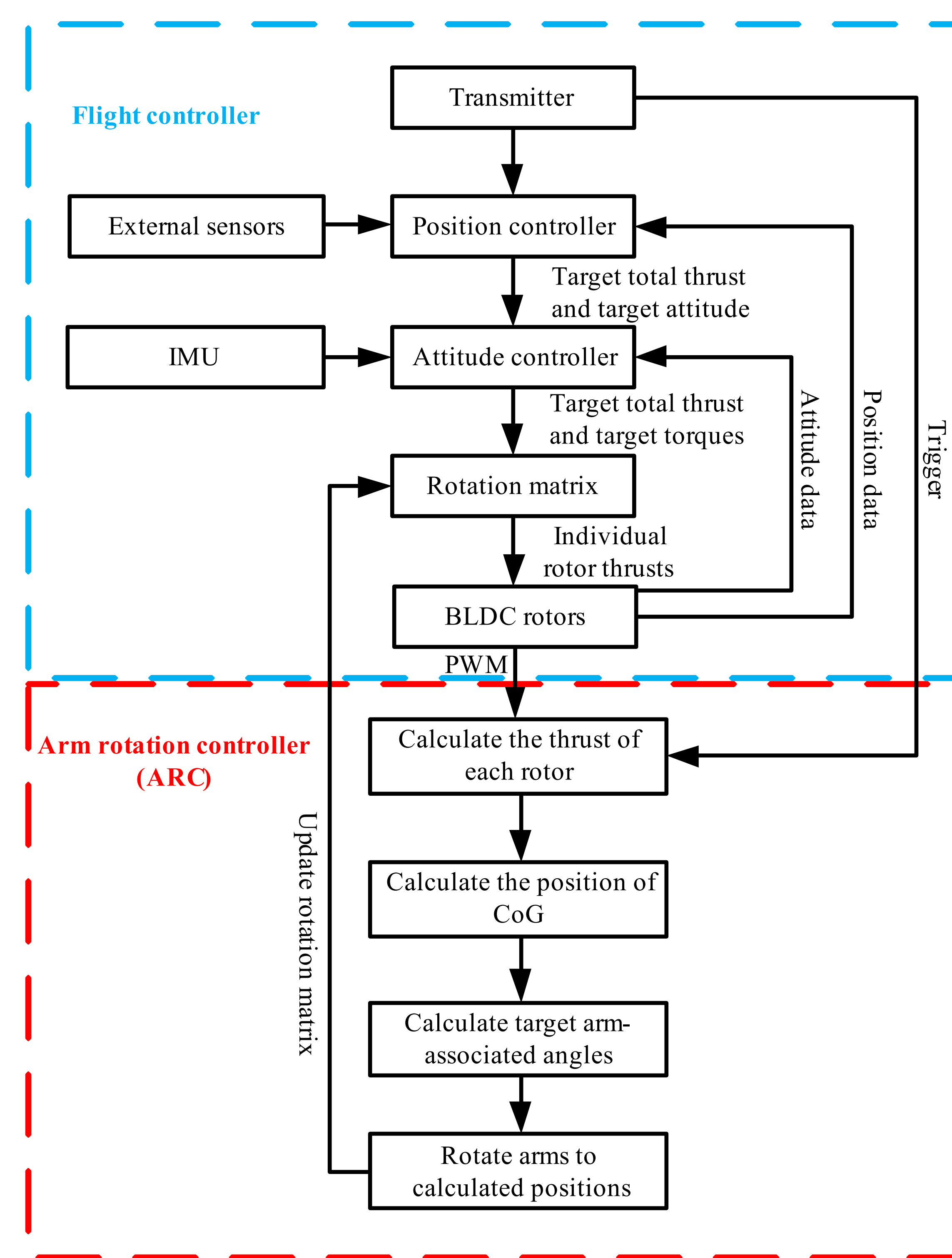


Dynamics notations of a quadrotor: (a) side view; and (b) top view

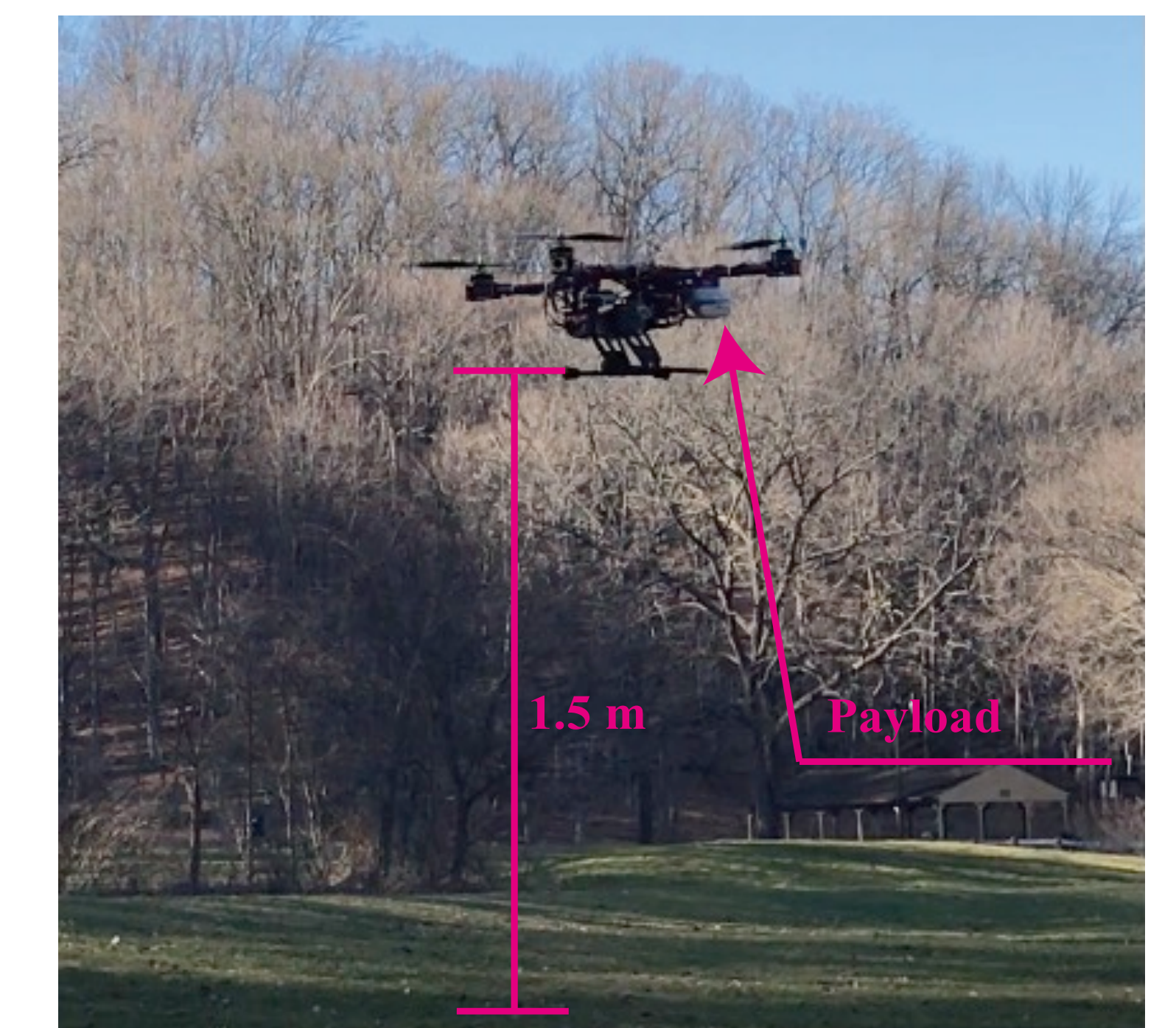
The position of a quadrotor's CoG in the body-fixed frame  $F_B$ :

$$\begin{cases} l_x = \frac{1}{mg} [a \sum_{i=1}^4 \sin \zeta_i F_i + W_1 \sum_{i=1}^2 (-1)^i F_i - W_2 \sum_{i=3}^4 (-1)^i F_i] \\ l_y = -\frac{1}{mg} [a \sum_{i=1}^4 \cos \zeta_i F_i + L \sum_{i=1}^2 F_i - L \sum_{i=3}^4 F_i] \end{cases}$$

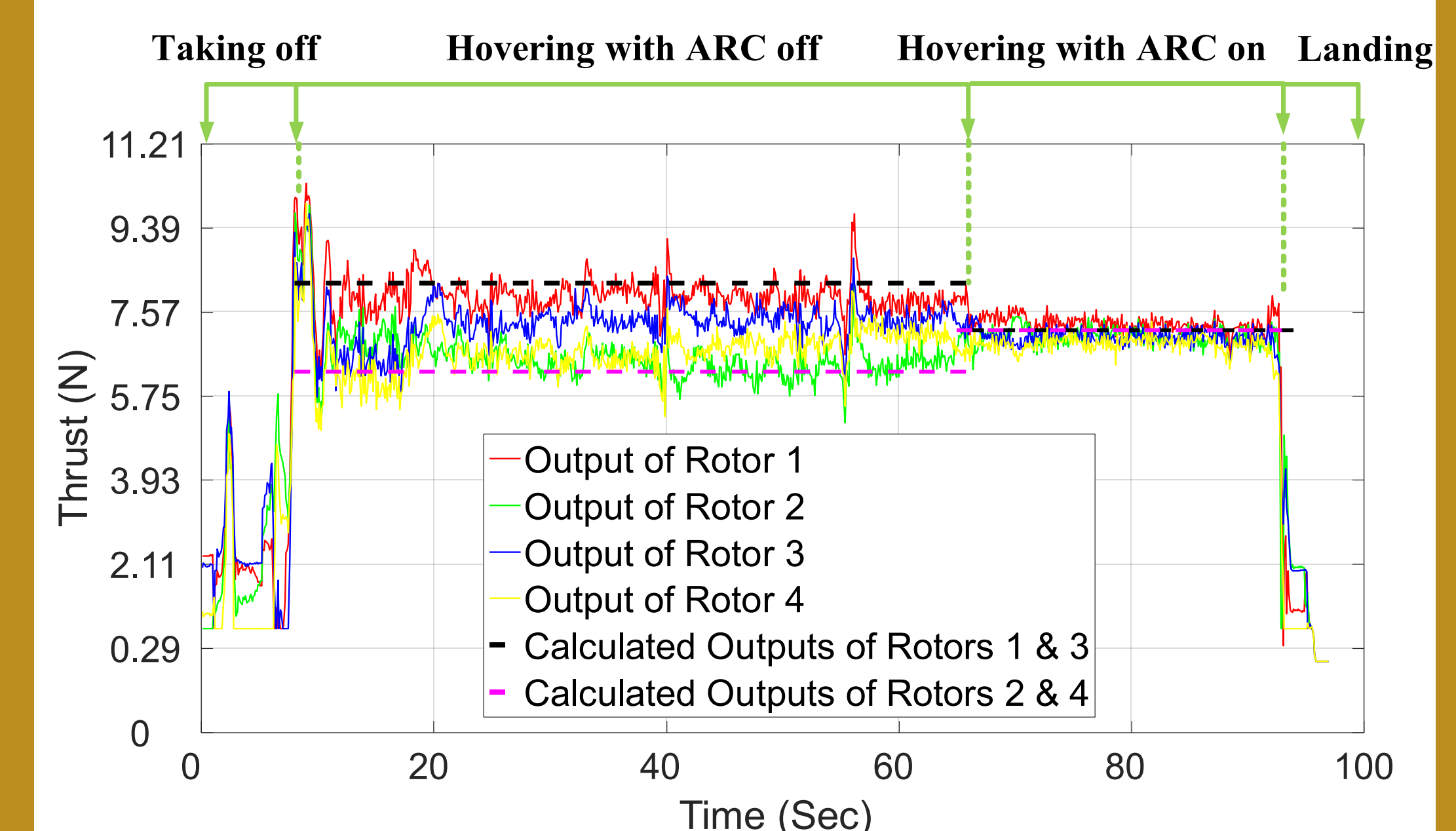
## Control Diagram and Simulation Results



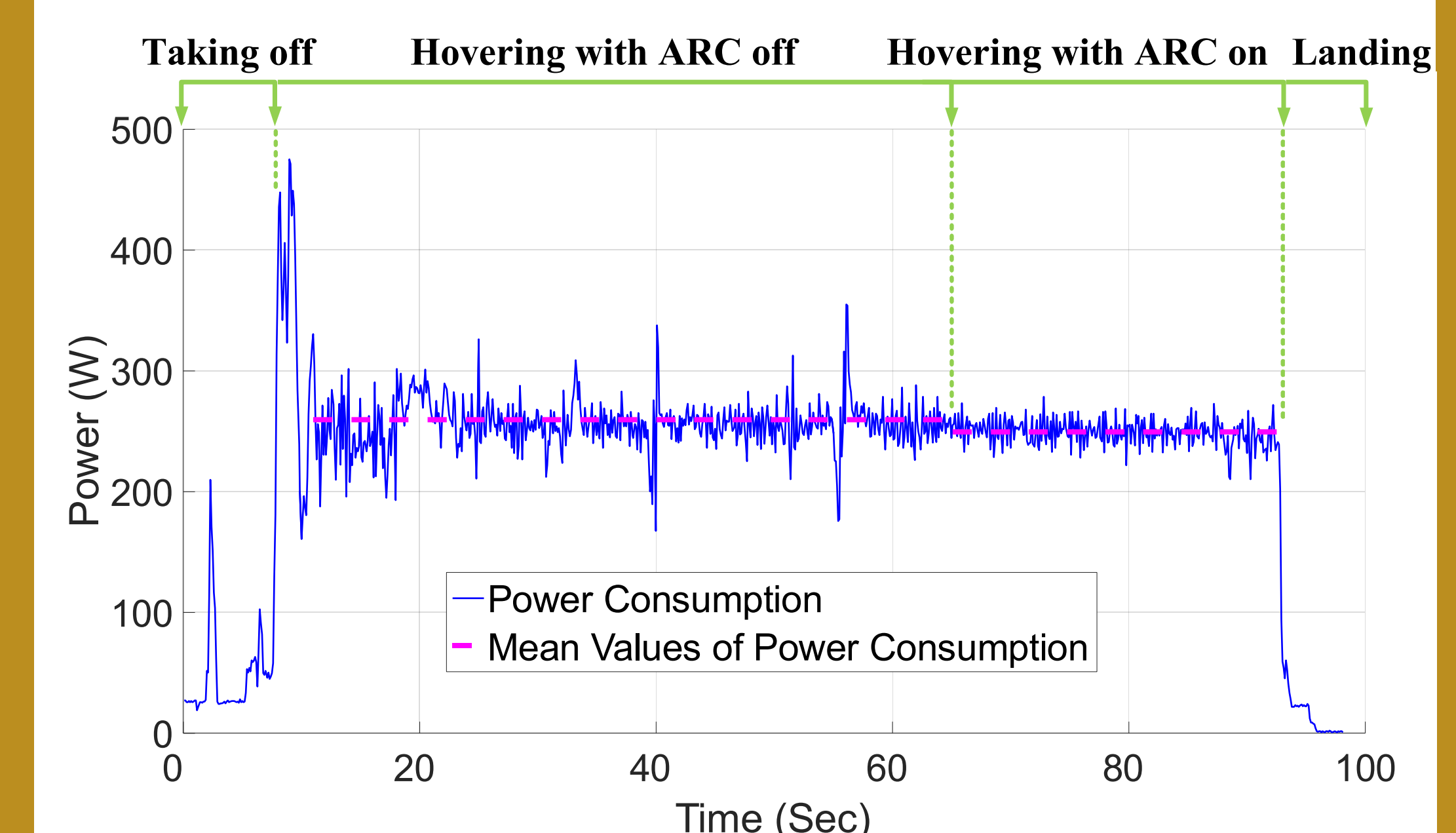
## Experiments and Validation



Field experiments



Thrusts of the QRA when hovering with a CoG offset of 0.04 m in x axis



Power consumption of the QRA when hovering with a CoG offset of 0.04 m in x axis

## Conclusion

- The proposed QRA can automatically compensate its CoG offset by rotating arms.
- Flying performances on stability and energy efficiency of the QRA are improved, compared to a QFA with the same arms, weight, rotors, and eccentric payloads.